

# Area triangolo e formule inverse con trigonometria

Geogebra, derive, cabri, excel

Vista Algebra

Angolo

- ☒  $\alpha = 1.17 \text{ rad}$
- ☒  $\beta = 0.97 \text{ rad}$
- ☒  $\gamma = 1.01 \text{ rad}$

Numero

- ☐  $d = 21.25$
- ☐  $e = 7.49$
- ☐  $f = 6.7$
- ☐  $g = 0.85$
- ☐  $h = 1.01$
- ☐  $i = 6.9$
- ☐  $j = 0.82$
- ☐  $k = 0.97$
- ☐  $l = 0.92$
- ☐  $m = 1.17$

Punto

- ☐  $A = (-0.58, -4.97)$
- ☐  $B = (6.32, -4.97)$
- ☐  $C = (2.06, 1.19)$

Segmento

- ☒  $a = 7.49$
- ☒  $b = 6.7$
- ☒  $c = 6.9$

Triangolo

- ☒  $\text{poli1} = 21.25$

Vista Grafica

noti 3 elementi, calcolare quarto

$$S = a \cdot b \cdot \sin(\gamma) / 2 = 21.25 \text{ (d)}$$

$$a = 2S / (b \cdot \sin(\gamma)) = 7.49 \text{ (e)}$$

$$b = 2S / (a \cdot \sin(\gamma)) = 6.7 \text{ (f)}$$

$$\sin(\gamma) = 2S / (a \cdot b) = 0.85 \text{ (g)} \quad \text{asin(g)}$$

$$c = 2s / (A \cdot \sin(\beta)) = 6.9 \text{ (i)}$$

$$\sin(\beta) = 2S / (a \cdot c) = 0.82 \text{ (j)}$$

$$\text{asin}(\beta) = .97 \text{ (k)}$$

$$\sin(\alpha) = 2 \cdot S / (b \cdot c) = 0.92 \text{ (l)}$$

$$\text{alfa} = \text{asin}(\alpha) = 1.17 \text{ (m)}$$

area triangolo

$$S = a \cdot b \cdot \sin(\gamma) / 2$$

$$S = a \cdot c \cdot \sin(\beta) / 2$$

$$S = b \cdot c \cdot \sin(\alpha) / 2$$



Protocollo di costruzione

N.

Nome

Definizione

Valore

14 Testo testo5

"S = a\*b\*sin(gamma) / 2 = 21.25 (d)"

15 Testo testo6

"noti 3 elementi, calcolare quarto"

16 Testo testo7

"a = 2S/(b\*sin(gamma)) = 7.49 (e)"

17 Numero e

2d / (b sin(gamma))

e = 7.49

18 Testo testo8

"b = 2S / (a\*sin(gamma)) = 6.7 (f)"

19 Numero f

2d / (a sin(gamma))

f = 6.7

20 Testo testo9

"sin(gamma) = 2S / (a\*b) = 0.85 (g)"

21 Numero g

2d / (a b)

g = 0.85

22 Numero h

asin(g)

h = 1.01

23 Testo testo10

"asin(g) = 1.01 rad (h)"

24 Testo testo11

"c = 2s / (A\*SIN(beta))=6.9 (i)"

25 Numero i

2d / (a sin(beta))

i = 6.9

26 Testo testo12

"sin(beta) = 2S / (a\*c) = 0.82 (j) asin(beta) = .97 (k)"

27 Numero j

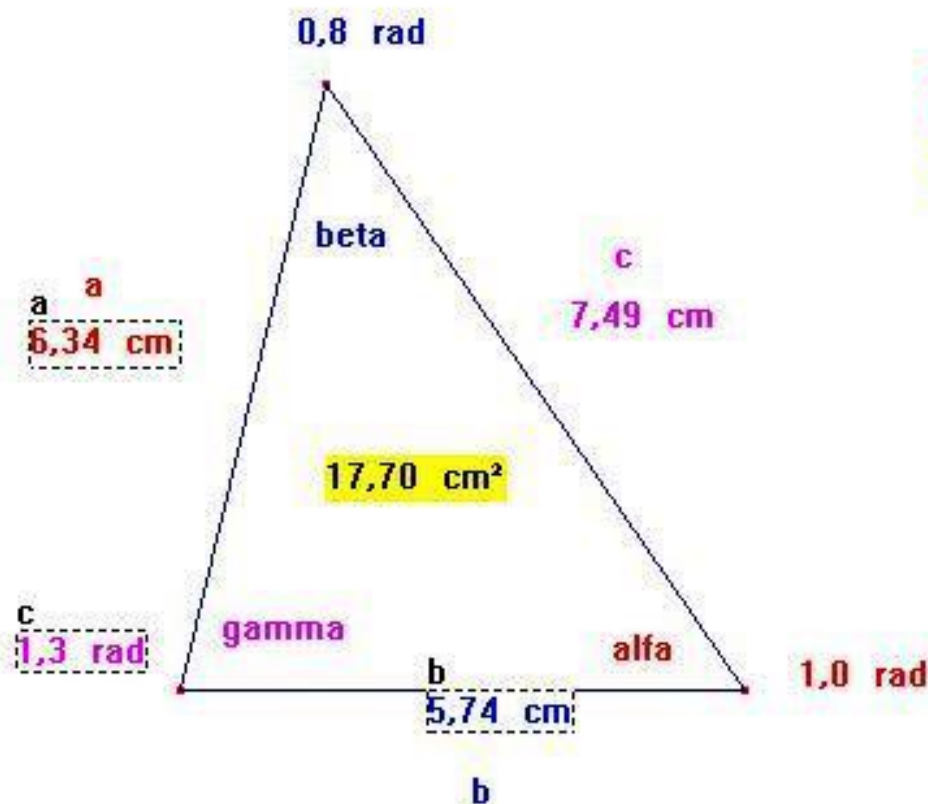
2d / (a c)

j = 0.82

28 Numero k

asin(j)

k = 0.97



calcolo area, noto a, b , gamma

Risultato:  $17.70 \text{ cm}^2$

noto a,c, beta

Risultato:  $17.70 \text{ cm}^2$

noto b, c , alfa

Risultato:  $17.70 \text{ cm}^2$

calcolo a

noto S, b, gamma

$$a = 2S / (b \cdot \sin(\gamma))$$

Risultato:  $6.34 \text{ cm}$

calcolo b

noto S, a , gamma

$$b = 2S / (a \cdot \sin(\gamma))$$

Risultato:  $5.74 \text{ cm}$

$$\text{area} = \text{lato1} \cdot \text{lato2} \cdot \sin(\text{angolo compreso}) / 2$$

$$S = a \cdot b \cdot \sin(\gamma) / 2$$

$$S = a \cdot c \cdot \sin(\beta) / 2$$

$$S = b \cdot c \cdot \sin(\alpha) / 2$$



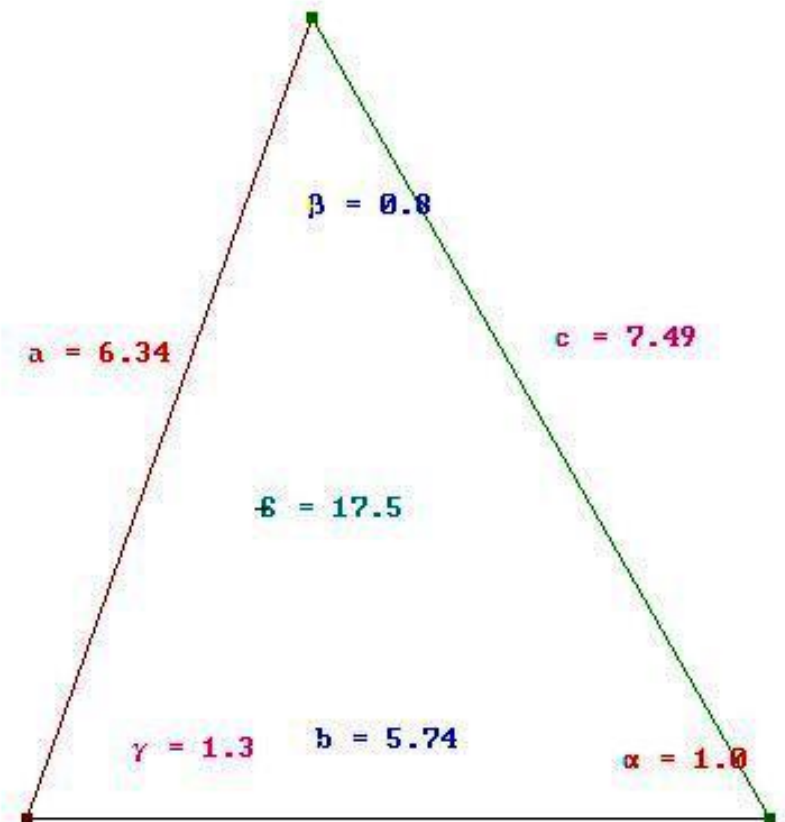
```

#1: "area triangolo, formule inverse"
#2: a := 6.34
#3: b := 5.74
#4: c := 7.49
#5:  $\alpha$  := 1
#6:  $\beta$  := 0.8
#7:  $\gamma$  := 1.3
#8: "....."
#9:  $\begin{bmatrix} -0.58 & -4.97 \\ 6.32 & -4.97 \end{bmatrix}$ 
#10:  $\begin{bmatrix} -0.58 & -4.97 \\ 2.06 & 1.19 \end{bmatrix}$ 
#11:  $\begin{bmatrix} 2.06 & 1.19 \\ 6.32 & -4.97 \end{bmatrix}$ 
#12: "....."
#13: "calcolo S "
#14: 
$$\frac{a \cdot b \cdot \sin(1.3)}{2}$$

#15: 17.5
#16: "....."
#17: "noti 3 elementi, calcolare quarto"

```

9

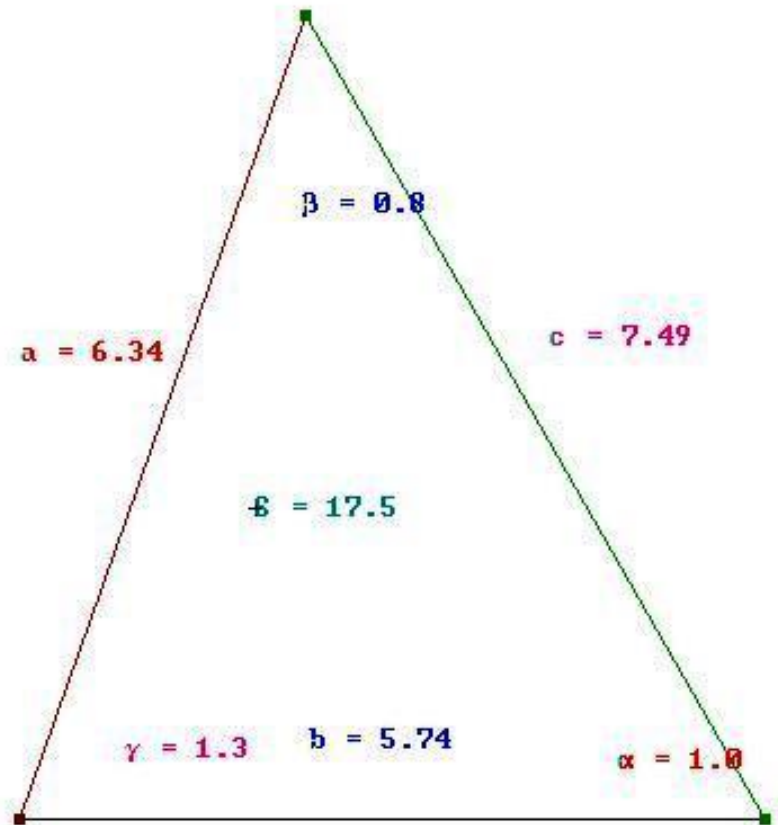


```

#16: .....
#17: "noti 3 elementi, calcolare quarto"
#18: "S = a*b*sin( $\gamma$ ) / 2"
#19: "S = a*c*sin( $\beta$ ) / 2 "
#20: "S = b*c*sin( $\alpha$ ) / 2"
#21: "....."
#22: s := 17.5
#23: "calcolo a"
#24: a :=  $\frac{2 \cdot s}{b \cdot \text{SIN}(1.3)}$ 
#25: 6.3
#26: "calcolo b"
#27: b :=  $\frac{2 \cdot s}{6.32978 \cdot \text{SIN}(1.3)}$ 
#28: 5.7
#29: "calcolo sin( $\gamma$ ) e asin( $\gamma$ ) = gamma"
#30:  $\frac{2 \cdot s}{6.32978 \cdot 5.74193}$ 
#31: 0.96
#32: ASIN(0.962962)
#33: 1.29
#34: "....."

```

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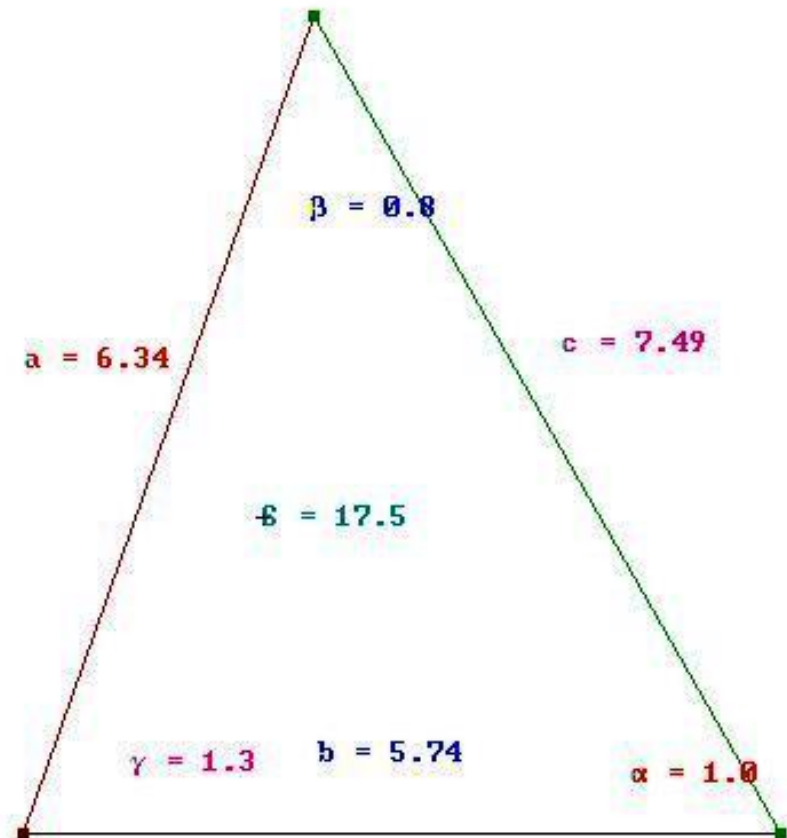
```

#34: "....."
#35: "S = a*c*sin(beta) / 2 "
#36: "calcolo c"
#37: 
$$\frac{2 \cdot s}{6.34 \cdot \sin(0.8)}$$

#38:  $\text{APPROX}\left(\frac{2 \cdot s}{6.34 \cdot \sin(0.8)}, 3\right)$ 
#39: 7.69
#40: "calcolo sin(beta), asin(beta) = beta"
#41:  $\frac{2 \cdot s}{6.34 \cdot 7.49}$ 
#42:  $\text{APPROX}\left(\frac{2 \cdot s}{6.34 \cdot 7.49}, 3\right)$ 
#43: 0.737
#44:  $\text{ASIN}(0.737)$ 
#45: 0.828
#46: "....."

```

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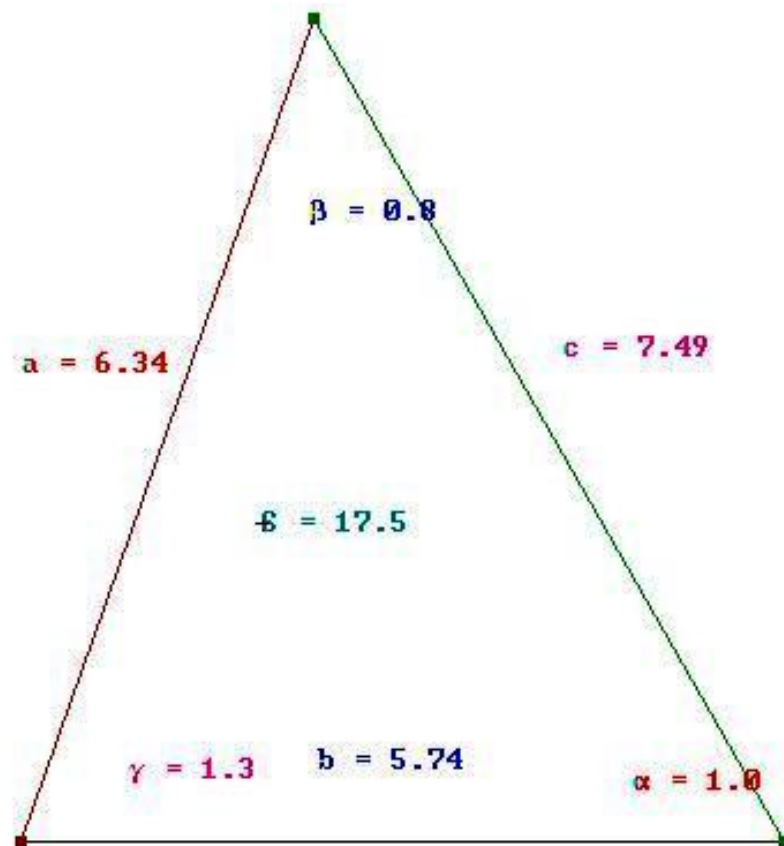
#46: .....
#47: "S = b*c*sin(α) / 2"
#48: "calcolo sin(α), asin(α) = alfa"
#49: 
$$\frac{2 \cdot s}{5.74 \cdot 7.49}$$

#50: 
$$\frac{25000}{30709}$$

#51: 0.814
#52: ASIN(0.814092)
#53: 0.951

```

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			alfa	beta	gamma		S1	17,53
6,34	5,74	7,49	1	0,8	1,3			

noti 3 elementi, calcolare quarto

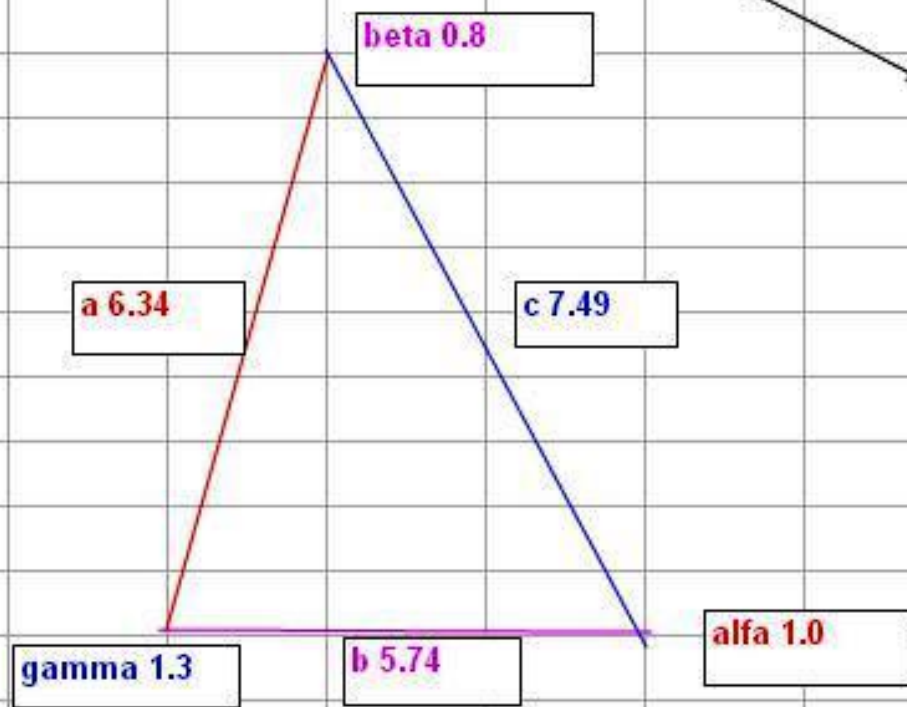
area triangolo

$$S1 = a \cdot b \cdot \sin(\gamma) / 2$$

$$S2 = a \cdot c \cdot \sin(\beta) / 2$$

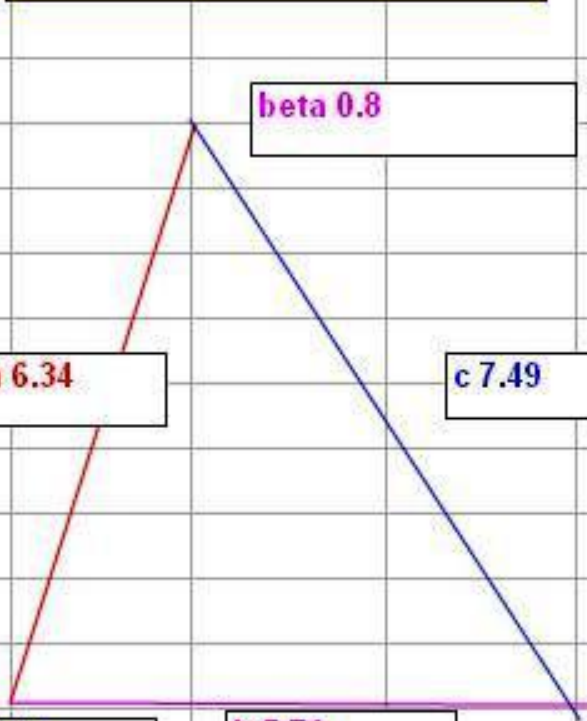
$$S3 = b \cdot c \cdot \sin(\alpha) / 2$$

a	6,34
b	5,74
'gamma	1,3
c	7,710011882
beta	0,830735835
alfa	0,953791907





1	a	b	alfa	beta	gamma		S1	=A2*B2*SEN(F2)/2
2	5,74	7,49	1	0,8	1,3			
3							noti 3 elementi, calcolare quarto	
4								
5	<div>area triangolo</div> <div><math>S1 = a \cdot b \cdot \text{sen}(\text{gamma}) / 2</math></div> <div><math>S2 = a \cdot c \cdot \text{sen}(\text{beta}) / 2</math></div> <div><math>S3 = b \cdot c \cdot \text{sen}(\text{alfa}) / 2</math></div>						a	=2*I1/(B2*SEN(F2))
6							b	=2*I1/(A2*SEN(F2))
7							'gamma	=ARCSEN(2*I1/(A2*B2))
8								
9							c	=2*I1/(A2*SEN(0,8))
10							beta	=ARCSEN(2*I1/(A2*C2))
11								
12							alfa	=ARCSEN(2*I1/(B2*C2))
13								
14								
15								
16								
17								
18								
19								
20								
21	gamma 1.3	b 5.74			alfa 1.0			



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$$c = 2s / (A \cdot \sin(\beta)) = 6.9 \text{ (i)}$$

$$\sin(\beta) = 2S / (a \cdot c) = 0.82 \text{ (j)}$$

$$\text{asin}(\beta) = .97 \text{ (k)}$$

$$\sin(\alpha) = 2 \cdot S / (b \cdot c) = 0.92 \text{ (l)}$$

$$\text{alfa} = \text{asin}(\alpha) = 1.17 \text{ (m)}$$

**area triangolo**

$$S = a \cdot b \cdot \sin(\gamma) / 2$$

$$S = a \cdot c \cdot \sin(\beta) / 2$$

$$S = b \cdot c \cdot \sin(\alpha) / 2$$

